## Ladislav Bican, Blas Torrecillas Relative exact covers

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Abstract: Recently Rim and Teply [11] found a necessary condition for the existence of  $\sigma$ -torsionfree covers with respect to a given hereditary torsion theory for the category *R*-mod. This condition uses the class of  $\sigma$ -exact modules; i.e. the  $\sigma$ -torsionfree modules for which every its  $\sigma$ -torsionfree homomorphic image is  $\sigma$ -injective. In this note we shall show that the existence of  $\sigma$ -torsionfree covers implies the existence of  $\sigma$ -exact covers, and we shall investigate some sufficient conditions for the converse.

**Keywords:** precover, cover, hereditary torsion theory  $\sigma$ ,  $\sigma$ -injective module,  $\sigma$ -exact module,  $\sigma$ -pure submodule **AMS Subject Classification:** 16D90, 16S90, 18E40