## Ladislav Bican Relatively exact modules

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**Abstract:** Rim and Teply [10] investigated relatively exact modules in connection with the existence of torsionfree covers. In this note we shall study some properties of the lattice  $\mathcal{E}_{\tau}(M)$  of submodules of a torsionfree module M consisting of all submodules N of M such that M/N is torsionfree and such that every torsionfree homomorphic image of the relative injective hull of M/N is relatively injective. The results obtained are applied to the study of relatively exact covers of torsionfree modules. As an application we also obtain some new characterizations of perfect torsion theories.

**Keywords:** Hereditary torsion theory  $\tau$ ,  $\tau$ -injective module,  $\tau$ -exact module, preradical, exact torsion theory, perfect torsion theory **AMS Subject Classification:** 16S90, 18E40, 16D80