Jiří Janáček Variance of periodic measure of bounded set with random position

Comment.Math.Univ.Carolin. 47,3 (2006) 443-455.

Abstract: The principal term in the asymptotic expansion of the variance of the periodic measure of a ball in \mathbb{R}^d under uniform random shift is proportional to the (d+1)st power of the grid scaling factor. This result remains valid for a bounded set in \mathbb{R}^d with sufficiently smooth isotropic covariogram under a uniform random shift and an isotropic rotation, and the asymptotic term is proportional also to the (d-1)-dimensional measure of the object boundary. The related coefficients are calculated for various periodic grids constructed from affine sets.

Keywords: periodic measure, variance AMS Subject Classification: 62J10, 62D05