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*On Mikheev's construction of enveloping groups*

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**Abstract:** Mikheev, starting from a Moufang loop, constructed a groupoid and reported that this groupoid is in fact a group which, in an appropriate sense, is universal with respect to enveloping the Moufang loop. Later Grishkov and Zavarnitsine gave a complete proof of Mikheev's results. Here we give a direct and self-contained proof that Mikheev's groupoid is a group, in the process extending the result from Moufang loops to Bol loops.

**Keywords:** Bol loop, Moufang loop, autotopism group, group with triality

**AMS Subject Classification:** 20N05

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