

Benjamin Cahen

Berezin-Weyl quantization for Cartan motion groups

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Abstract: We construct adapted Weyl correspondences for the unitary irreducible representations of the Cartan motion group of a noncompact semisimple Lie group by using the method introduced in [B. Cahen, *Weyl quantization for semidirect products*, Differential Geom. Appl. **25** (2007), 177–190].

Keywords: semidirect product, Cartan motion group, unitary representation, semisimple Lie group, symplectomorphism, coadjoint orbit, Weyl quantization, Berezin quantization

AMS Subject Classification: 22E45, 22E46, 22E70, 22E15, 81S10, 81R05

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