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Commutative subloop-free loops

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Abstract: We describe, in a constructive way, a family of commutative loops of odd order, $n \geq 7$, which have no nontrivial subloops and whose multiplication group is isomorphic to the alternating group A_n .

Keywords: loops, multiplication group, alternating group

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