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*C*¹-smoothness of Nemytskii operators on Sobolev-type spaces of periodic functions

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Abstract: We consider a class of Nemytskii superposition operators that covers the non-linear part of traveling wave models from laser dynamics, population dynamics, and chemical kinetics. Our main result is the *C*¹-continuity property of these operators over Sobolev-type spaces of periodic functions.

Keywords: Nemytskii operators, Sobolev-type spaces of periodic functions, *C*¹-smoothness

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