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The dual space of precompact groups

Abstract: For any topological group G the dual object $\widehat{G}$ is defined as the set of equivalence classes of irreducible unitary representations of G equipped with the Fell topology. If G is compact, $\widehat{G}$ is discrete. In an earlier paper we proved that $\widehat{G}$ is discrete for every metrizable precompact group, i.e. a dense subgroup of a compact metrizable group. We generalize this result to the case when G is an almost metrizable precompact group.

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