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 *$E_1$ -degeneration and  $d'd''$ -lemma*

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**Abstract:** For a double complex  $(A, d', d'')$ , we show that if it satisfies the  $d'd''$ -lemma and the spectral sequence  $\{E_r^{p,q}\}$  induced by  $A$  does not degenerate at  $E_0$ , then it degenerates at  $E_1$ . We apply this result to prove the degeneration at  $E_1$  of a Hodge-de Rham spectral sequence on compact bi-generalized Hermitian manifolds that satisfy a version of  $d'd''$ -lemma.

**Keywords:**  $\partial\bar{\partial}$ -lemma; Hodge-de Rham spectral sequence;  $E_1$ -degeneration; bi-generalized Hermitian manifold

**AMS Subject Classification:** 55T05, 53C05

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