

Thomas Jech

*Convergence
in Boolean algebras*

and

submeasures

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Abstract: A Boolean algebra carries a strictly positive exhaustive submeasure if and only if it has a sequential topology that is uniformly Fréchet.

Keywords: Boolean algebra; exhaustive submeasure; sequential topology; uniformly Fréchet topology

AMS Subject Classification: 03G05, 28A60

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