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*Metric trees in the Gromov–Hausdorff space*

Comment.Math.Univ.Carolin. 64,1 (2023) 73–82.

**Abstract:** Using the wedge sum of metric spaces, for all compact metrizable spaces, we construct a topological embedding of the compact metrizable space into the set of all metric trees in the Gromov–Hausdorff space with finite prescribed values. As its application, we show that the set of all metric trees is path-connected and all its nonempty open subsets have infinite topological dimension.

**Keywords:** metric tree; Gromov–Hausdorff distance

**AMS Subject Classification:** 53C23, 51F99

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