## Raquel Crescimbeni Singular integral characterization of nonisotropic generalized BMO spaces

Comment.Math.Univ.Carolin. 48,2 (2007) 225-238.

Abstract: We extend a result of Coifman and Dahlberg [Singular integral characterizations of nonisotropic  $H^p$  spaces and the F. and M. Riesz theorem, Proc. Sympos. Pure Math., Vol. 35, pp. 231–234; Amer. Math. Soc., Providence, 1979] on the characterization of  $H^p$  spaces by singular integrals of  $\mathbb{R}^n$  with a nonisotropic metric. Then we apply it to produce singular integral versions of generalized BMO spaces. More precisely, if  $T_{\lambda}$  is the family of dilations in  $\mathbb{R}^n$  induced by a matrix with a nonnegative eigenvalue, then there exist 2n singular integral operators homogeneous with respect to the dilations  $T_{\lambda}$  that characterize BMO<sub> $\varphi$ </sub> under a natural condition on  $\varphi$ .

**Keywords:** singular integral, nonisotropic generalized BMO **AMS Subject Classification:** Primary 42B30; secondary 42B99