

Alexander Arhangel'skii
*The Baire property in remainders
of topological groups and other results*

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Abstract: It is established that a remainder of a non-locally compact topological group G has the Baire property if and only if the space G is not Čech-complete. We also show that if G is a non-locally compact topological group of countable tightness, then either G is submetrizable, or G is the Čech-Stone remainder of an arbitrary remainder Y of G . It follows that if G and H are non-submetrizable topological groups of countable tightness such that some remainders of G and H are homeomorphic, then the spaces G and H are homeomorphic. Some other corollaries and related results are presented.

Keywords: Baire property, σ -compact, Čech-complete space, compactification, Čech-Stone compactification, Rajkov complete, paracompact p -space

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