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*Spectral analysis for rank one perturbations
of diagonal operators in non-archimedean Hilbert space*

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Abstract: The paper is concerned with the spectral analysis for the class of linear operators $A = D_\lambda + X \otimes Y$ in non-archimedean Hilbert space, where D_λ is a diagonal operator and $X \otimes Y$ is a rank one operator. The results of this paper turn out to be a generalization of those results obtained by Diarra.

Keywords: spectral analysis, diagonal operator, rank one operator, eigenvalue, spectrum, non-archimedean Hilbert space

AMS Subject Classification: 44A35, 42A85, 42A75

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