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On weakly monotonically monolithic spaces

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Abstract: In this note, we introduce the concept of weakly monotonically monolithic spaces, and show that every weakly monotonically monolithic space is a D-space. Thus most known conclusions on D-spaces can be obtained by this conclusion. As a corollary, we have that if a regular space X is sequential and has a point-countable wcs^*-network then X is a D-space.

Keywords: D-space, sequential space, wcs^*-network, weakly monotonically monolithic space
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