

**Ryotaro Sato**

*Ratio Tauberian theorems for relatively bounded functions and sequences in Banach spaces*

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**Abstract:** We prove ratio Tauberian theorems for relatively bounded functions and sequences in Banach spaces.

**Keywords:** ratio Tauberian theorem,  $\gamma$ -th order Cesàro integral, Laplace integral,  $\gamma$ -th order Cesàro sum, Abel sum

**AMS Subject Classification:** 40E05, 47A35

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