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G-nilpotent units of commutative group rings

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Abstract: Suppose R is a commutative unital ring and G is an abelian group. We give a general criterion only in terms of R and G when all normalized units in the commutative group ring RG are G -nilpotent. This extends recent results published in [Extracta Math., 2008–2009] and [Ann. Sci. Math. Québec, 2009].

Keywords: group rings, normalized units, nilpotents, idempotents, decompositions, abelian groups

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