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Extending the ideal of nowhere dense subsets of rationals to a P-ideal

Abstract: We show that the ideal of nowhere dense subsets of rationals cannot be extended to an analytic P-ideal, F_σ ideal nor maximal P-ideal. We also consider a problem of extendability to a non-meager P-ideals (in particular, to maximal P-ideals).

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