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A new Lindelöf space with points G_δ

Abstract: We prove that $\diamondsuit^*$ implies there is a zero-dimensional Hausdorff Lindelöf space of cardinality $2^{\aleph_1}$ which has points G_δ. In addition, this space has the property that it need not be Lindelöf after countably closed forcing.

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