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An existence and approximation theorem for solutions of degenerate quasilinear elliptic equations

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Abstract: The main result establishes that a weak solution of degenerate quasilinear elliptic equations can be approximated by a sequence of solutions for non-degenerate quasilinear elliptic equations.

Keywords: degenerate quasilinear elliptic equations; weighted Sobolev spaces

AMS Subject Classification: 35J62, 35J70, 35D30

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