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*Classification of spaces of continuous functions on ordinals*

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**Abstract:** We conclude the classification of spaces of continuous functions on ordinals carried out by Górak [Górak R., *Function spaces on ordinals*, Comment. Math. Univ. Carolin. **46** (2005), no. 1, 93–103]. This gives a complete topological classification of the spaces  $C_p([0, \alpha])$  of all continuous real-valued functions on compact segments of ordinals endowed with the topology of pointwise convergence. Moreover, this topological classification of the spaces  $C_p([0, \alpha])$  completely coincides with their uniform classification.

**Keywords:** space of continuous functions; pointwise topology; homeomorphism of function spaces; uniform homeomorphism; ordinal number

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