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Spectra of uniformity

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Abstract: We study some limitations and possible occurrences of uniform ultrafilters on ordinals without the axiom of choice. We prove an Easton-like theorem about the possible spectrum of successors of regular cardinals which carry uniform ultrafilters; we also show that this spectrum is not necessarily closed.

 ${\bf Keywords:}$ uniform ultrafilter; axiom of choice; measurable cardinal; strongly compact cardinal

AMS Subject Classification: 03E25, 03E55, 03E35

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