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Artinianness of formal local cohomology modules

Comment.Math.Univ.Carolin. 60,2 (2019) 177 –185.

Abstract: Let $\mathfrak{a}$ be an ideal of Noetherian local ring $(R, \mathfrak{m})$ and M a finitely generated R-module of dimension d. In this paper we investigate the Artinianness of formal local cohomology modules under certain conditions on the local cohomology modules with respect to $\mathfrak{m}$. Also we prove that for an arbitrary local ring $(R, \mathfrak{m})$ (not necessarily complete), we have $\mathrm{Att}_R(\mathfrak{F}^d_\mathfrak{a}(M)) = \mathrm{MinV}(\mathrm{Ann}_R\mathfrak{F}^d_\mathfrak{a}(M))$.

Keywords: formal local cohomology; local cohomology
AMS Subject Classification: 13D45, 13E99

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