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*True preimages of compact or separable sets  
for functional analysts*

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**Abstract:** We discuss various results on the existence of ‘true’ preimages under continuous open maps between  $F$ -spaces,  $F$ -lattices and some other spaces. The aim of the paper is to provide accessible proofs of this sort of results for functional-analysts.

**Keywords:** preimage; open map; complete metric space;  $F$ -space;  $F$ -lattice; compact set; uniformly open map; surpositive operator; lower semicontinuous set-valued map

**AMS Subject Classification:** 46A16, 46A30, 54E35, 54E40, 54E45, 54E50, 54D65, 54C10

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