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Noncompact perturbation of nonconvex noncompact sweeping process with delay

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Abstract: We prove an existence theorem of solutions for a nonconvex sweeping process with nonconvex noncompact perturbation in Hilbert space. We do not assume that the values of the orient field are compact.

Keywords: nonconvex sweeping process; functional differential inclusion; uniformly ϱ -prox-regular set

AMS Subject Classification: 34A60, 34B15, 47H10

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