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Three small results on normal first countable linearly H-closed spaces

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Abstract: We use topological consequences of PFA, $\mathsf{MA}_{\omega_1}(\mathsf{S})[\mathsf{S}]$ and PFA(S)[S] proved by other authors to show that normal first countable linearly H-closed spaces with various additional properties are compact in these models.

Keywords: linearly H-closed space; normal space; first countable space; forcing axiom
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