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On Szymański theorem on hereditary normality of $\beta\omega$

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Abstract: We discuss the following result of A. Szymański in "Retracts and non-normality points" (2012), Corollary 3.5.: If F is a closed subspace of ω^* and the π-weight of F is countable, then every nonisolated point of F is a non-normality point of ω^*. We obtain stronger results for all types of points, excluding the limits of countable discrete sets considered in "Some non-normal subspaces of the Čech–Stone compactification of a discrete space" (1980) by A. Błaszczyk and A. Szymański. Perhaps our proofs look "more natural in this area".

Keywords: Čech–Stone compactification; non-normality point; butterfly-point; countable π-weight
AMS Subject Classification: 54D15, 54D35, 54D40, 54D80, 54E35, 54G20

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