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On the Jacobson radical of strongly group graded rings

Abstract: For any non-torsion group G with identity e, we construct a strongly G-graded ring R such that the Jacobson radical $J(R_e)$ is locally nilpotent, but $J(R)$ is not locally nilpotent. This answers a question posed by Puczyłowski.