Pavel Drábek, Zakaria Moudan, Abdelfettah Touzani Nonlinear homogeneous eigenvalue problem in \mathbb{R}^N : nonstandard variational approach

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Abstract: The nonlinear eigenvalue problem for p-Laplacian

$$\{\ -div(a(x)|\nabla u|^{p-2}\nabla u)=\lambda g(x)|u|^{p-2}u\ \text{in}\ \mathbb{R}^N, u>0\ \text{in}\ \mathbb{R}^N, \lim_{|x|\to\infty}u(x)=0,$$

is considered. We assume that 1 and that <math>g is indefinite weight function. The existence and $C^{1,\alpha}$ -regularity of the weak solution is proved.

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