## E. Harboure, O. Salinas, B. Viviani Relations between weighted Orlicz and $BMO_{\phi}$ spaces through fractional integrals

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Abstract: We characterize the class of weights, invariant under dilations, for which a modified fractional integral operator  $I_{\alpha}$  maps weak weighted  $\operatorname{Orlicz}-\phi$  spaces into appropriate weighted versions of the spaces  $BMO_{\psi}$ , where  $\psi(t)=t^{\alpha/n}\phi^{-1}(1/t)$ . This generalizes known results about boundedness of  $I_{\alpha}$  from weak  $L^p$  into Lipschitz spaces for  $p>n/\alpha$  and from weak  $L^{n/\alpha}$  into BMO. It turns out that the class of weights corresponding to  $I_{\alpha}$  acting on weak- $L_{\phi}$  for  $\phi$  of lower type equal or greater than  $n/\alpha$ , is the same as the one solving the problem for weak- $L^p$  with p the lower index of Orlicz-Maligranda of  $\phi$ , namely  $\omega^{p'}$  belongs to the  $A_1$  class of Muckenhoupt.

**Keywords:** theory of weights, Orlicz spaces, BMO spaces, fractional integrals **AMS Subject Classification:** Primary 42B25